

Constraining cosmological parameters in FLRW metric with lensed GW+EM signals

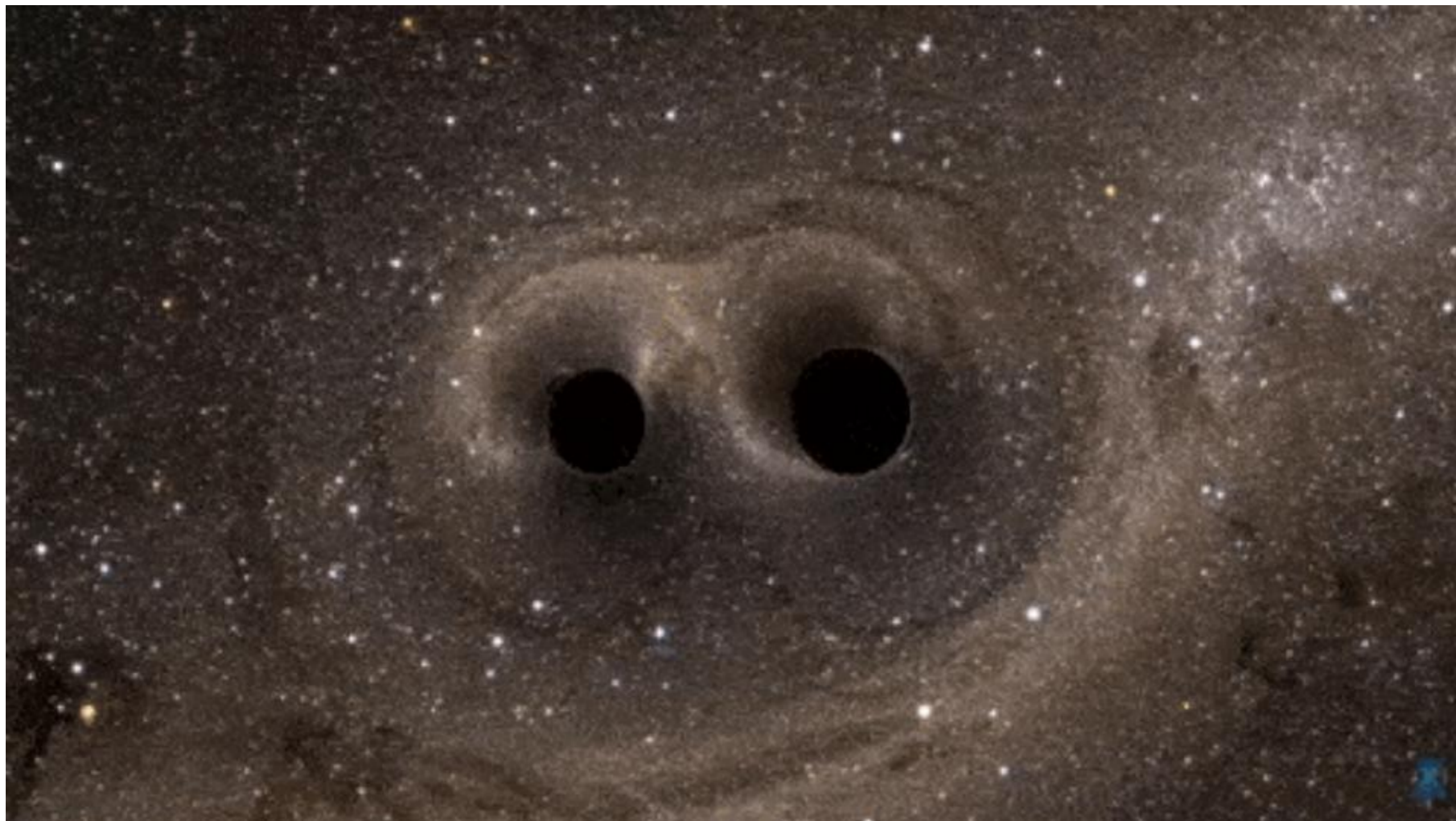
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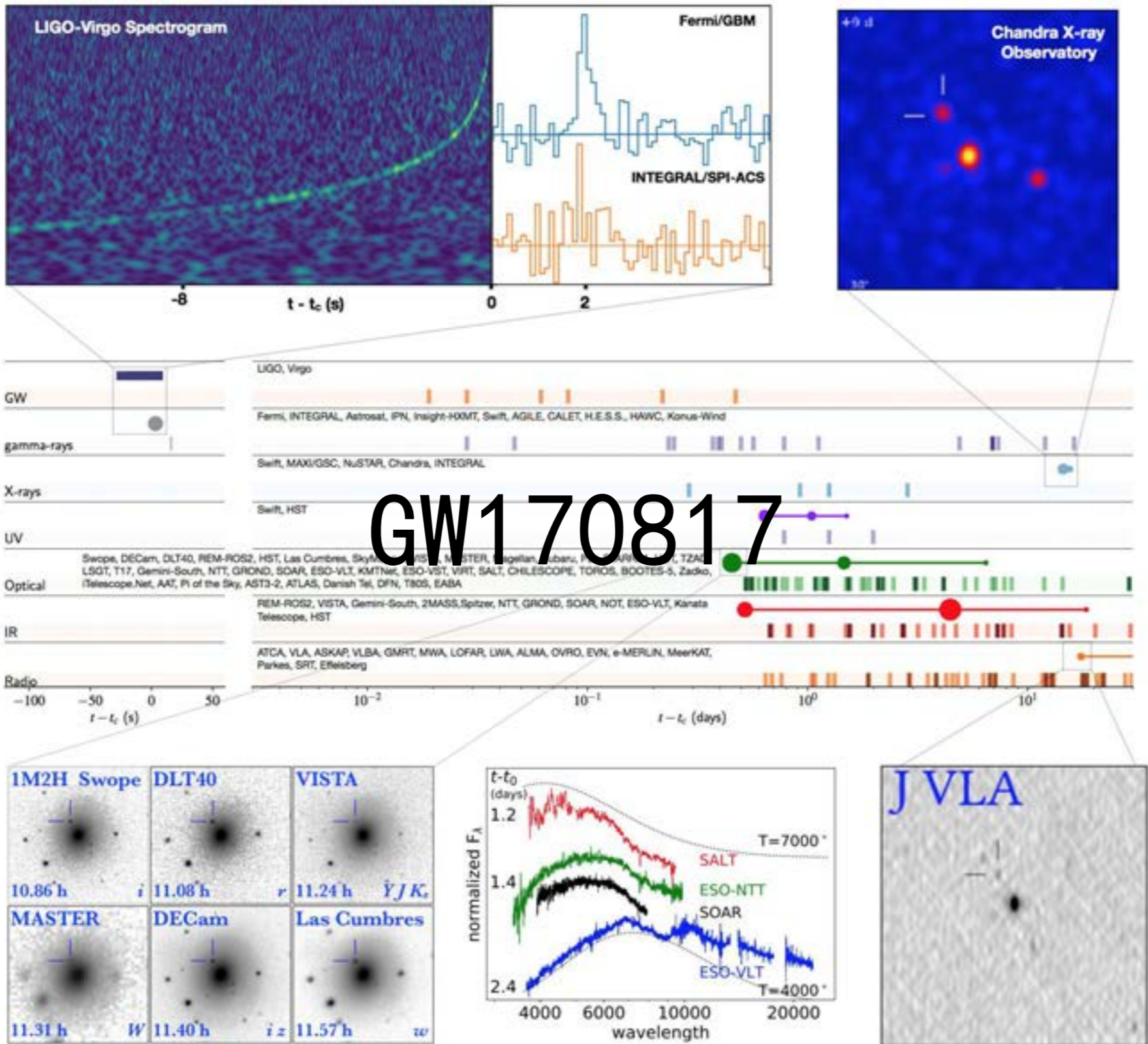






GW150914

B. P. Abbott et al. 2016



EM



EM+GW



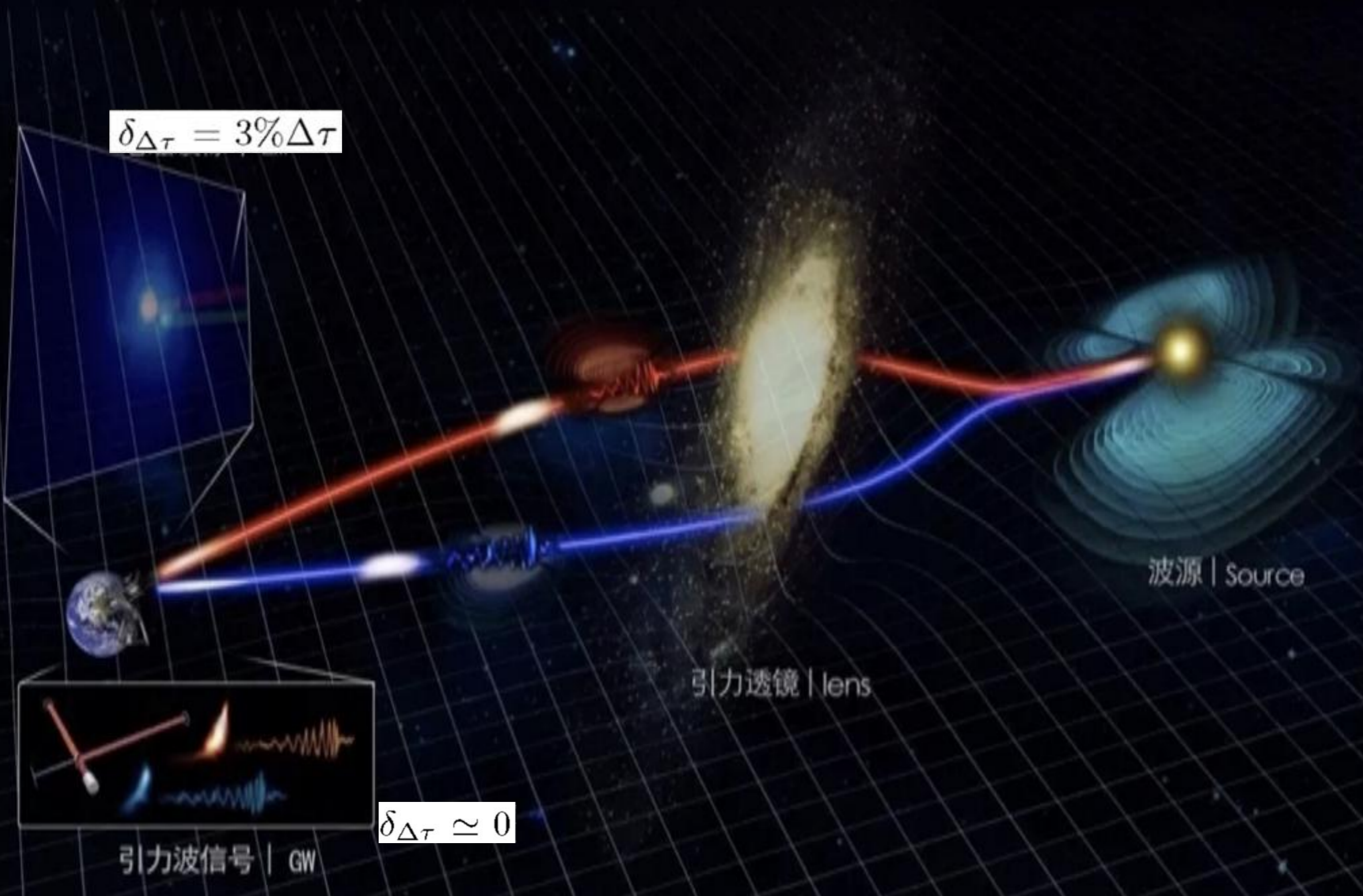
$$\delta_{\Delta\tau} = 3\% \Delta\tau$$

波源 | Source

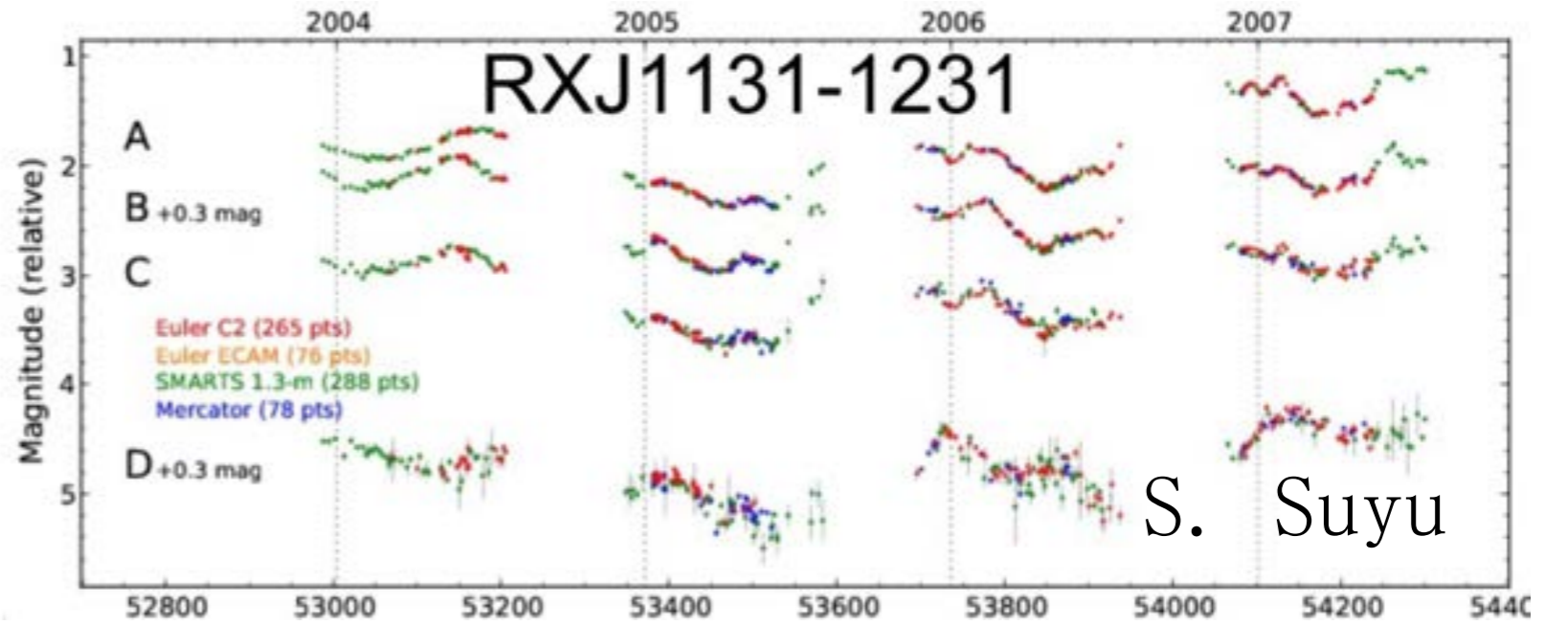
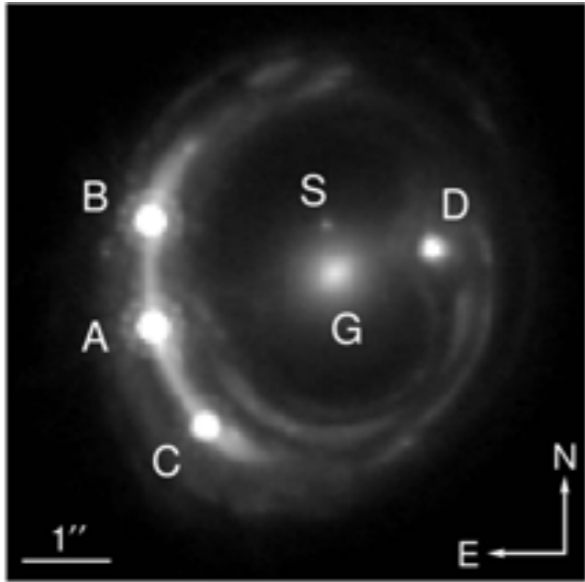
引力透镜 | lens

$$\delta_{\Delta\tau} \approx 0$$

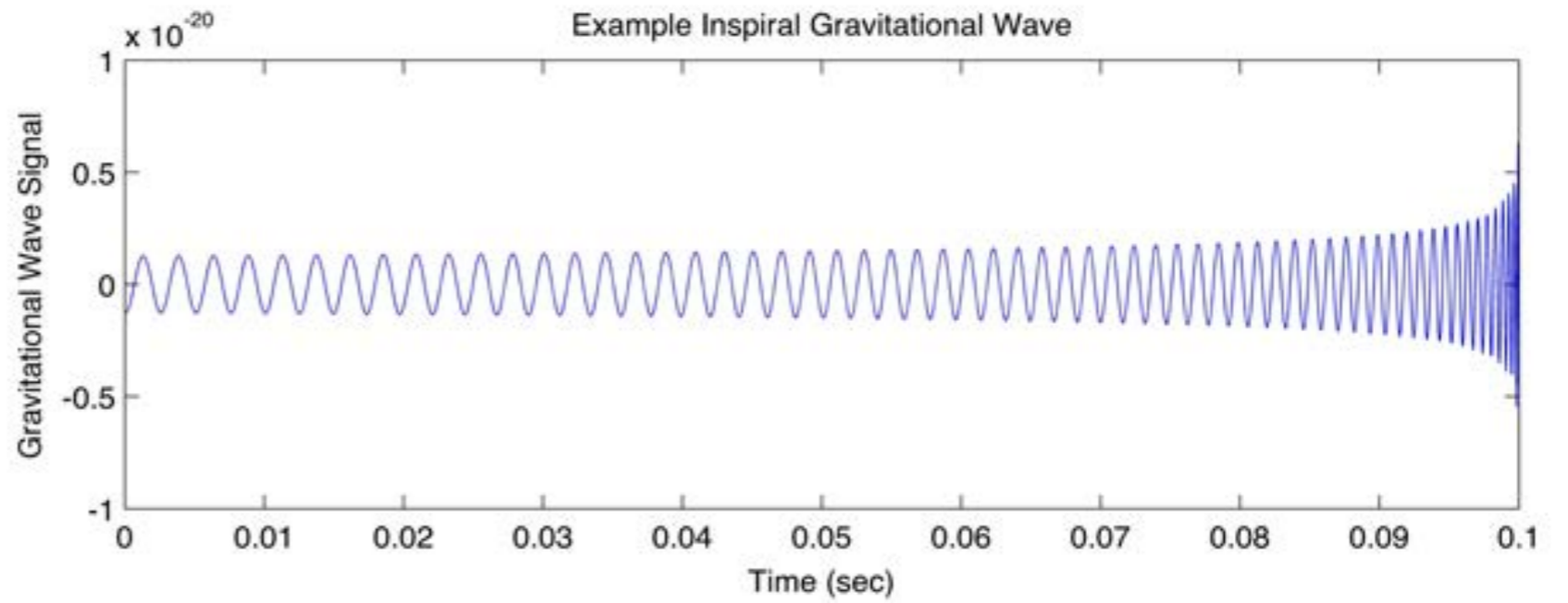
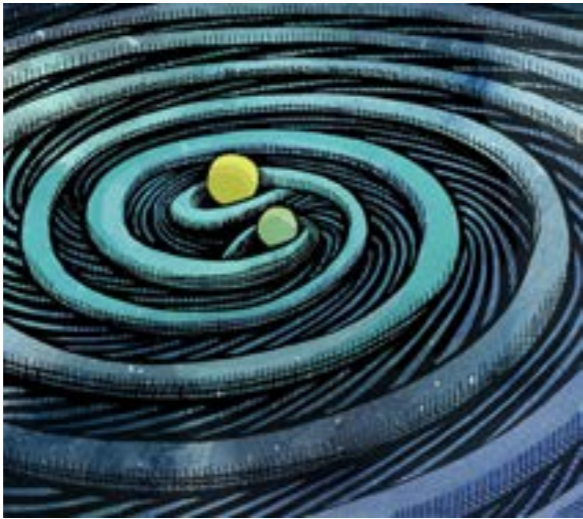
引力波信号 | GW



EM



GW



- 1. Ding et al.(2015): ET will detect 50 – 100 lensed GWs per year**
- 2. Liao et al.(2017): just 10 such systems can provide a Hubble constant uncertainty of 0.68%**
- 3. Fan et al.(2017): lensed GW+EM systems can be used to measure the speed of gravitational waves**
- 4. Wei et al.(2017): strongly lensed GW-EM systems can provide stringent constraints on parameters of Dark energy equation of state**



Lens redshift Source redshift

$$D_{\Delta t} = \frac{D_A(z_l)D_A(z_s)}{D_A(z_l, z_s)}$$

$$D_{\Delta t}(\text{observation}) = \frac{\Delta t}{(1 + z_l)\Delta\phi}$$

$$\Delta\phi_{i,j} = \left[\frac{(\theta_i - \beta)^2}{2} - \psi(\theta_i) - \frac{(\theta_j - \beta)^2}{2} + \psi(\theta_j) \right]$$

Fermat potential difference

$$D_{\Delta t}(\text{observation}) = D_{\Delta t}(\text{theory})$$

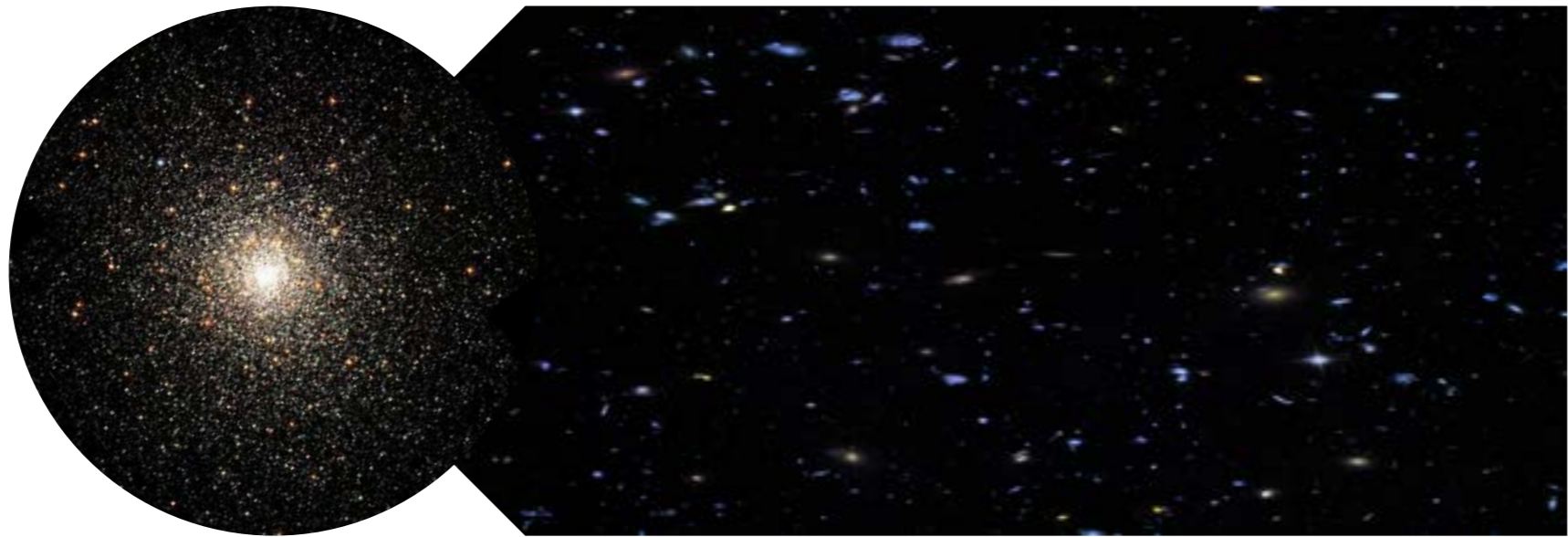
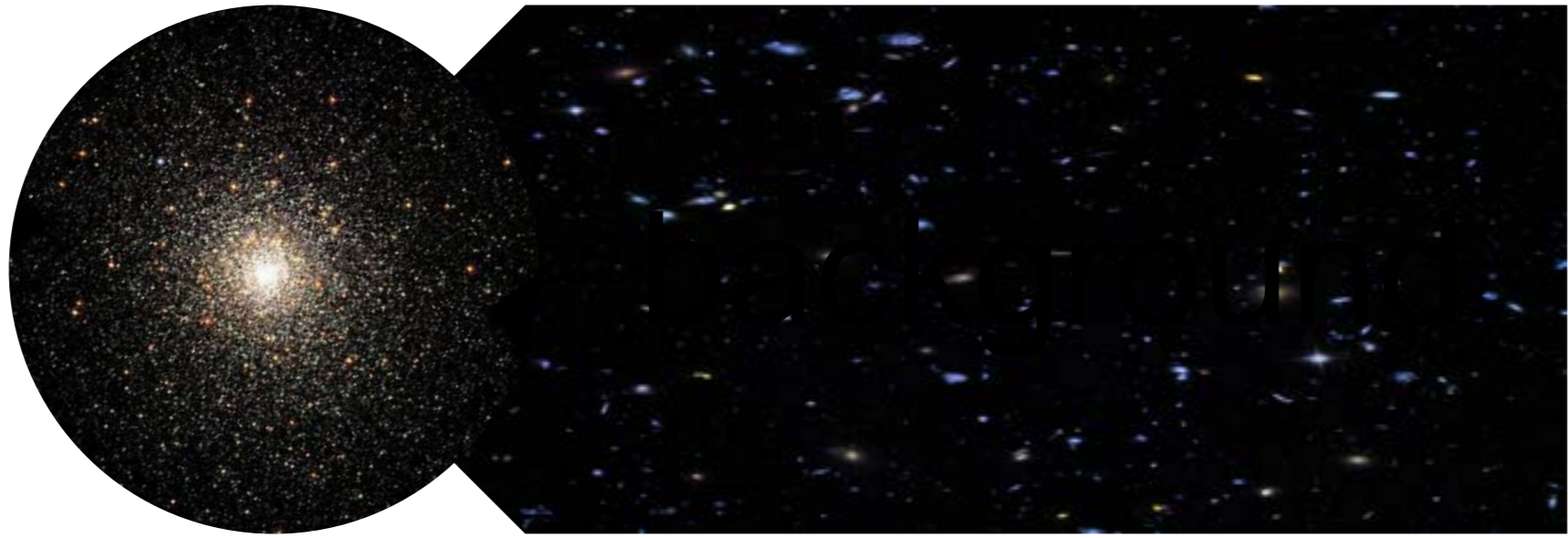
observed quantities ($z_l, z_s, \Delta t, \Delta\phi, D_L$)

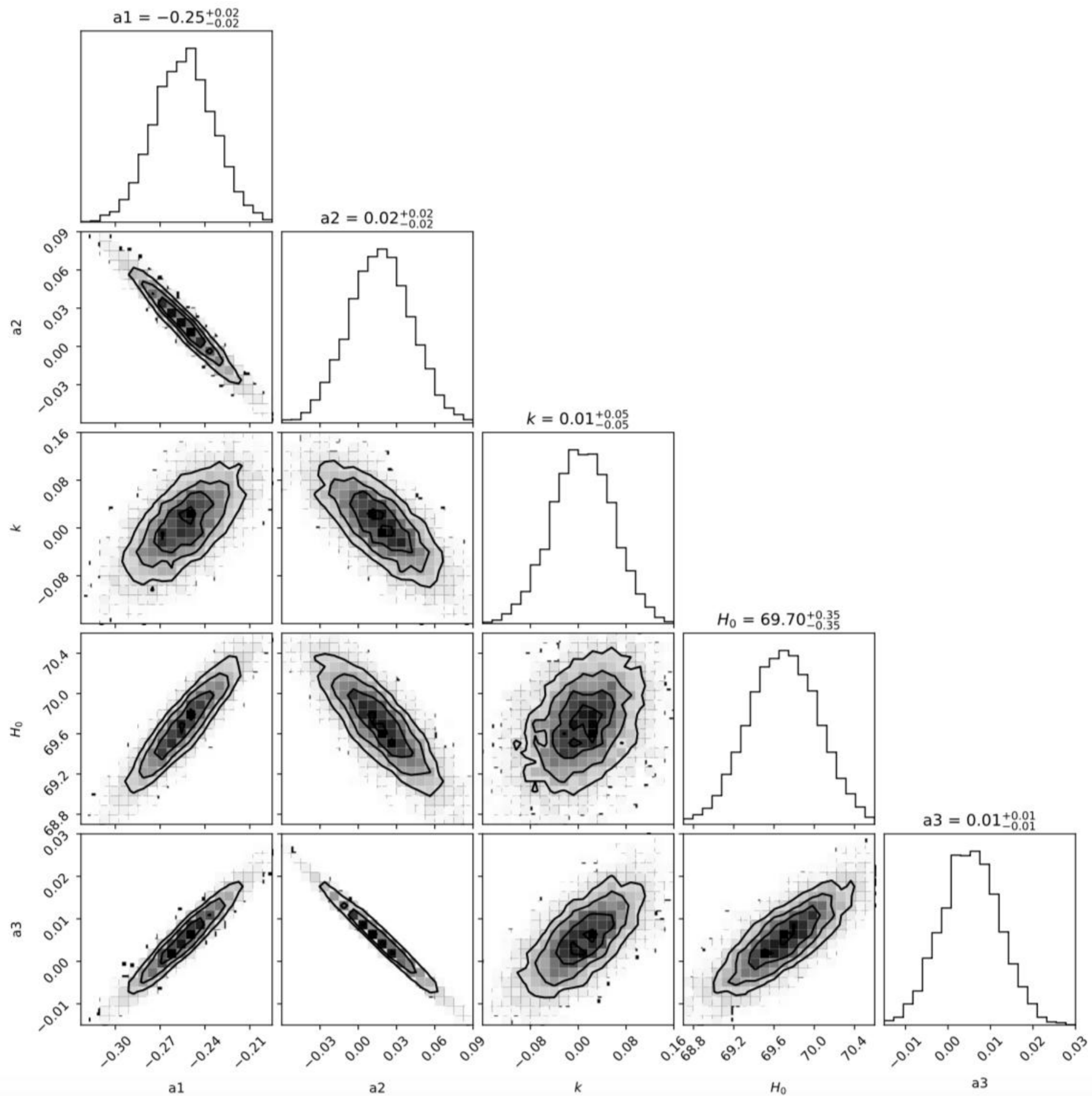
$$D_{\Delta t}(\text{theory}) = \frac{1}{(1 + z_l)(T(z_l) - T(z_s))}$$

$$T(z) = \frac{1}{d(z)} \sqrt{1 - kd(z)^2}$$

$$d(z) = z + a_1z^2 + a_2z^3 + a_3z^4$$

theoretical values ($k, d(z), H_0$)





<https://arxiv.org/abs/1901.10638>

	No.	$a1$	$a2$	$a3$	k	H_0
lensed quasar	300	$-0.24^{+0.04}_{-0.04}$	$0^{+0.06}_{-0.06}$	$0.01^{+0.03}_{-0.02}$	$0^{+0.05}_{-0.06}$	$69.86^{+0.53}_{-0.53}$
lensed GW+EM	10	$-0.25^{+0.02}_{-0.02}$	$0.02^{+0.02}_{-0.02}$	$0.01^{+0.01}_{-0.01}$	$0.01^{+0.05}_{-0.05}$	$69.7^{+0.35}_{-0.35}$

Summary

- *Strongly lensed GW-EM systems combine highly accurate time delay from GW signals with redshift and image from EM counterparts.*
- *In the future, strongly lensed GW-EM systems can be applied to do precision cosmology.*
- *Establish a complete set of lensed GW-EM numerical simulation is necessary.*

Thank
You